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"Al" rapy relat theme AND ANGLE OF ATTACK VARIATION.

S. E. Lechenbruch

ABSTRACT

In any tose bombing maneuver in which eight line and flight line prior to pull-up do not coincide, an impact error results. The amount of this error per mil of sight error is given by Equation (2) or Figure 2. The error may be corrected with the MPI adjustment dial by an amount determined from Equation (9) or Figure 3.

Sight misalignments depend on (a) the fixed orientation of the eight with respect to the airplane, and (b) the orientation of the airplane with respect to its flight line. The latter is the <u>angle of attack</u>, which is increased by a decrease in either dive angle or air speed, and therefore varies considerably since decreases in dive angle are usually accompanied by decreases in air speed. Differences in angle of ettack may be determined from Equation (13) or from the nomogram of Figure 5.

If the effect of m sight elenlignment is counteracted at some mean value of altitude, dive angle, and air speed, by an PI adjustment $\Delta T_c / T_c$, the impact error at another altitude, dive angle, and air speed is the algebraic sum of that due to (a) the difference between the angles of attack at the mean value and second value of dive angle and air speed, (b) the sight error for which adjustment was made, and (c) the $\Delta T_c / T_c$ adjustment itself. Hereis (b) and (c) are is opposite directions and partially offset each other, whereas (a) may affect the result considerably in either direction.

When the sight line is below the flight line, such greater bombing so-curacy is schieved by a fixed readjustment of the sight-itself then by an MPI adjustment. Under certain conditions it may be advantageous to overadjust the sight conswhat, bringing sight line above flight line, and currecting the resulting cleal symment by a $\Delta T_{\rm c}/T_{\rm c}$ adjustment.

INTROD CTION

In toes bombing, the flight path of the eirplane before pull-up is assumed to be a collision course, i.e., a straight path directed toward the target. Since the flight path is determined in practice by means of a eight which is kept fixed on the target, the sound path can be a collision course only if the plane constantly flies along the eight line.

Sight misslignments may arise from the fact that for any aircraft the sight is usually adjusted to be correct for shooting of the machine gume. This adjustment is not suitable for bombs area bombs leave the sircraft in a direct control of the sir

5006-1

tion tangent to the flight path, while bullets, because of their high murale velocity, leave in the direction in which the gums are pointing. Differences between the eight and flight lines may also occur as a result of variations in the angle of attack, which for any type of plane depends on its weight, velocity, and dive angle. The errors resulting from such misalignments, and means of correcting them, form the subject of this paper.

Figure 1 represents the flight of plane and bomb for the case in which the line of flight makes a constant angle ϕ with the sight line, the sight being kept fixed on the target K' until pull-up. The vectors marked ϕ represent instantaneous directions of the sight line, directed toward the target; those marked ϕ , making an angle ϕ with the ϕ -vectors, represent the corresponding instantaneous directions of flight. It will be noted that the path ϕ is slightly concave upward; it would be concave downward if ϕ had the opposite sense. For small angles ϕ , however, very little sharifice of accuracy results from assuming that are ϕ is straight.

If A is the first altitude point, the values of dive angle (A), time-to-target (\mathbb{R}_{+}), and airspeed (V), which are fed into the computer are determined by conditions along AO, assuming that the dive angle gyro is sligned with respect to flight line. Barring other errors, therefore, the release time $Te^{*}(PV)$ will be so determined as to cause a hit at H, on the extension of AO, the corresponding slant range OH being $S = V \cdot T_C$. The horisontal impact arror due to the misslighment is $S = V \cdot T_C$.

The angle ϕ is considered positive when the sight line is above the flight line, and the error ξ positive when it represents an impact beyond the target. In Figure 1, ϕ is positive and ξ negative.

INPACT MEROR RESULTING FROM SIGHT MISALIGHDE: T

The exact relation between ϕ and δ is obtained at once by application of the sine law to triangle $OHK^!$

When | | is small compared with of , a close approximation is

whene in radians. The amount by which (?) is in error as compared to the exact expression (1), is given approximately by the ratio of the thus for values in to 1° or 17 mils, (2) is accurate to within 5% for of as small as 20°, and to within 10% for of = 10°.

Pieure 2 is a contour men, in polar co-ordinates, of the relation between S and C corresponding to severa) fixed values of the ratio - 6/6, being the impact error caused by wight error 6. The corresponding rectangular coordinates of points on these curves are the horizontal range (Scales) and second altitude (Ran Saint); hence the curves may be considered pictorially as the loci of spatial release points corresponding to given - 6/6, the

target being at the origin. The value of $-\delta_{\phi}/\phi$ for a given release point may be obtained by interpolation between consecutive curves, so that Figure 2 is in one sense a graph of $-\delta_{\phi}/\phi$ as a function of release point. (Several other context maps of this type are included in this paper.

On converting (2) to rectangular coordinates, it becomes apparent that the curves of Figura 2 are aros of circles which pass through the origin, with centers on the vertical axis and radii- $\frac{1}{2} \frac{1}{2} \frac{1}{2}$

According to the exact equation (1), δ_{ϕ} is actually proportional, not to ϕ , but to $I/(\cot\phi-\cot\phi)$, which differs significantly from ϕ in radians when α and $I/\phi I$ are of comparable magnitude, i.e., for very small α or very large ϕ . The graph of Figure 2 therefore become accurate for all values of α and ϕ if the feet per mil values with which the curves are labeled are considered as values, not of $-\delta_{\phi}/\phi_{mils}$. but of $-1000\delta_{\phi}/(\cot\phi-\cot\alpha)$.

CORRECTION FOR SIGHT MISALIGHMENT BY MPI ADJUSTMENT A To /To

The arror due to mon-soincidence of eight and flight lines would be eliminated, causing a hit on the terget K' (Fig. 1), if the T_C value fed into the computer were adjusted to correspond to a target at H' instead of H. This would seen a relative increase $C_C = \Delta T_C / T_C$ (or a relative decrease $-\Delta T_C / T_C$), where $V\Delta T_C = HH'$, and $\Delta T_C / T_C = HH'/OH$.

Application of the sine law to the triangle HH'K', on the small assumption that the parabolic arc K'H' has negligible curvature, yields at eace

1.1.
$$E_c = \frac{V\Delta T_c}{S} = -\frac{\delta \Theta \text{ and}}{S}$$
, or $\delta / E_c = -S / \Theta \text{ and}$, (4)

where Θ_g' is the angle between trajectory and collision course at their intersection, and

$$\Theta = \frac{\operatorname{pin}(\alpha + O_i)}{\operatorname{pina} \operatorname{pino}_i} = \cot O_i + \cot \alpha \tag{6}$$

Formula (4) or its equivalent has been encountered in every problem involving correction of an impact error. The value of @ in terms of 5, V, o, and K (where Kg is pull-up acceleration) is implied in Report On-EP-105, Equa-

^{*} The negative sign in (4) holds only when C_c represents the adjustment required to offset the error G. When it represents that required to produce the error G, the sign of the right member of (4) is positive.

tions (9), (3), and (6):

$$= \frac{\sqrt{M/K} \tan \alpha}{-1 + \sqrt{1+2B}} \left(\sqrt{M/K} + \sqrt{1+2B} \right) + \sec \alpha \csc \alpha, \tag{60}$$

there is a K - coa a, and

$$A = \frac{54}{\sqrt{2}}, \frac{1}{12} \text{ and }$$
 (7)

Substitution of (1) into (4) gives the correction required to effect a given ϕ :

$$E_{c} = \frac{V\Delta T_{c}}{S} = + \frac{\Theta}{\cot \phi - \cot \phi} = \frac{\cot \Theta_{i} + \cot \phi}{\cot \phi - \cot \phi}$$
 (8)

Again, when $|\phi|$ is small compared with α , a close approximation is

$$\epsilon_c * \Theta \Phi$$
, or $\epsilon_c = \Theta$ (9)

The gosuracy of (9) relative to (6) is similar to that given in the statement fellowing equation (2).

A formule equivalent to (A) was already derived in Report OD-27-69 in the course of a general discussion of angles.

Squation (9) may be solved for S by solving (6b) for $\sqrt{1+2B}$ and using the relations $B = \frac{1}{2} \left[\left(\frac{1}{1+2B} \right)^2 \cdot 1 \right]$, $S = B \cdot V^2 \, K/Mg$ aim a

The result is

$$S = \frac{V^2}{g_{aumo}} \frac{K}{M} \frac{N}{D} (1 + \frac{1}{2} \frac{N}{D})$$
 (10)

where

Figure 8 is a contour map, based on (10), of \mathcal{E}_{C} / \mathcal{G} , as percent-change in \mathcal{T}_{C} per mill of eight error, as a function of release point. \mathcal{H} is held constant at the value 8, the varieties of \mathcal{E}_{C} / \mathcal{G} vial \mathcal{H} being quite small. The range and altitude scales involve it factors; which is unity when V=350 ° knote. In nearly—size with (10), which implies that \mathcal{G}_{C} was an V=250 for fixed \mathcal{E}_{C} / \mathcal{G}_{C} and \mathcal{H}_{C} , the graph may be used for any air speed V by substituting $\mathcal{H}_{C}=(V/350)$ knote). At 350 and 300 knote, $\mathcal{H}_{C}=(V/350)$ knote, \mathcal{H}_{C}

Actually 250 | 2 C 853.6 kmote.

As in the case of Figure 3, Figure 3 as such becomes inaccurate for very small \varnothing or very large ϕ , but becomes accurate for all \varnothing and φ if the "% per mil" figures given are considered as values, not of ε / mile, but of 1000 ε (cst ϕ - cst ω).

According to (9), Figure 3 may also be interpreted as a coatour map of the much-used function @. When used as such, the "\$ per mil" figures must be reconverted into "units per radian" by multiplication by .01/.001 = 10. The curve marked 0.85 per mil, for example, is as well the locus of @ = 8.

Figure 4 is a contour map, based on (4), of $|S_C|$ as a function of release point, S_C being the impact error corresponding to the change S_C . From Figure 4 may be read the smount of displacement of the impact point per percent change in T_C , both changes having the same algebraic size. Furthermore, the reciprocals of the $|S_C|$ figures on the curves represent the percent change in T_C required to offset each foot of impact error; and when so interpreted, S_C and S_C have opposite algebraic sizes. The graph is of a general nature, applicable not only to the eight error problem but to all problems involving correction of an impact error by adjustment of T_C . The air speed factor $\eta = (1.7500 \text{ kmots})^2$ is included in the range, altitude, and contour scales.

By comparing equations (2), (4), and (9), and noting that $(E_c/\phi)(S/E_c) = S/\phi$, it is seen that for any given release point the value of S/ϕ , as given by Figure 2, is the product of the values of E_c/ϕ , as in Figure 3, and of S/ϕ_c as in Figure 4. The curves of Figure 4 have been constructed, not by solving (4) for 5 directly — this would have yielded a set of cubic equations — but father from Figures 2 and 3, by determining points of intersection of curves in Figure 3 with circles of appropriate radii similar to those in Figure 2.

VARIATION OF AUGLE OF ATTACK

Application of the preceding section, and of Figures 2 and 3, requires that the value of the sight error of for any specific cases, or at least the difference between of values for two specific cases, be known. The effective sight error, however, depends not only on the fixed orientation of the sight with respect to the airplane, but also on the angle of attack, or orientation of the plane with respect to its flight line. The variation of the latter with air speed and dive angle is appreciable and must be taken into account.

The angle of attack $\phi \alpha$ is given by the formula

$$\phi_{\alpha} = \frac{c w \cos d}{V^2} - k$$

(12)

where W is the gross weight of the plane, and C and K are constants for any one plane. The value of K also depends on the choice of a reference line in the airplane, and for purposes of calculating differences in angles of attack

eme may set \$20 with no less of generality:

$$\phi_{\alpha} = \frac{c w \cos \alpha}{V^2} \tag{13}$$

It is found generally that C has the same value for all planes of a series, as THM-1 and THM-10.

The memogram of Figure 5 gives this relative angle of attack ϕ_{a} , as in (13), on a function of C, W, V and A. The collibrations on lines I, II, IV, and VI, have been determined from values of log C, log V, log V, and log $CO \leftarrow CI$, respectively. Points on line III have been pre-dotermined for each plane at its membral weight $^{\circ}$, thus obvioting the use of lines I and II whenever the green weight is approximately mention.

Lines III through VII have been so spaced that V and C may be entered in either order. This property is illustrated by the sample appearing on the nonogram. The point on line V marked "767, 350 kmete" may be joined with reversal points in turn on line VI to obtain ϕ_{∞} on line VII for different dive angles at the fixed air speed; or the point marked "767, 40° may be joined with points on line IV to obtain ϕ_{∞} for different air speeds at the fixed dive angle. The relative convenience of the two methods depends on whether one is concerned more with variation of ϕ_{∞} with dive angle or with air speed.

According to (13), the rugle of attack, while independent of range, is increased by a decrease in either air speed or dive angle. Hence the range of variation in ϕ_{α} for any given plane is widened by the fact that decreases in dive angle are in practice usually accompanied by decreases in air speed.

APPLICATION OF THEORY

The preceding sections suggest two alternative methods of correcting for eight misalignment at a given range, dive angle, and air speed: (a) direct adjustment of the sight until flight and night lines coincide; or (b) integrator adjustment, i.e., shanging To by a percentage Cg determined from Figure 3.

The adjustment required, however, depends in either case on the values of α and Y, and in case (b) on S as well. Since it is not familie to make frequent readjustments of either type in any one plane, in practice a <u>fixed</u> adjustment must be made, such as would completely offset the sight error at some chosen intermediate or model value of S, α , and V. At other values an impact error will generally result, the magnitude of which depends on the method used — a fixed sight adjustment, a fixed integrator adjustment, or some combination of the two. The most efficient method is of course the one which minimizes this impact dispersion.

The following example illustrates the results of a fixed interrator adjustment: The night installed in an PSF plane at nominal weight (12,400 lbs.) is missligned by -30 mile at elant range $\frac{\pi}{2}$ = 7500 feet, dive angle $\frac{\pi}{2}$ = 40°, and air speed $\frac{\pi}{2}$ = 350 kmete. A fixed percent-adjustment in $\frac{\pi}{2}$ is unde in an amount

^{*} As obtained from OSED Reports 2264 (CIT/UNO 3), 2271-2275 (CIT/UNC 4-8), 2882 (CIT/UNC 25), and 2347 (CIT/UNC 28).

ist sufficient to effect the -20 mil sight error at (5, A, V), orusing this. It is desired to determine the resulting impact error at shart range 5 = 12,000 res3, dive angle A = 60, and air speed A = 375 knote.

From Figure 3 the required percent-adjustment in T_c per mil at 7300 feet, 40°, and 350 knote (Point \overline{p}) is $C_c/\phi = 0.75\%$ per mil, so that for $\phi = -20$ mils the fixed adjustment is $C_c = -15.0\%$. In other words, under these conditions a 15% decrease in T_c , by itself, would displace the impact point by an amount equal and opposite to the displacement which would result from a -20 mil sight error alone.

At another range, dive angle, and eir speed there two displacements, while oppositely directed, will generally be unequal in magnitude; and in addition, the angle of attack will generally be different. Thus the impact error et (S_i , C_i , V_i) will be the algebraic sum of three displacement components: (a) the difference Q_i between the engles of ettack et (Q_i , V_i) and (C_i , V_i) is a change in eight error and therefore causes an impact displacement Q_i ; (b) the original eight error Q_i ; (c) the edjustment C_i = -15%, by itself, would give a negative (short-of-target) error Q_i .

- (a) The difference in angle of attack is determined from Figure 5. For an F6F plane at nominal weight, this nonogram gives $\phi_a = 14.9$ mile at $\alpha = 40^\circ$. V = 380 knots, and 8.5 ° mile at $\alpha_1 = 60^\circ$. V = 375 knots. Hence $\Delta \phi_{cl} = -6.4$ mile. But from Figure 2, at $\alpha_1 = 60^\circ$ and $\Delta_1 = 12,000$ feet (Point Q), $-\Delta /\phi =$ eleut 14 feet per mil, so that the impact displacement due to change in angle of attack is $\Delta_1 = 490$ feet.
- (b) From this same ratio $-\delta/\phi$ =14 feet per mil, it follows that the -20 mil eight error in itself seases an impact error δ_0 = $-\sqrt{200}$ feet.
- (c) Finally, at 12,000 feet, 60° , and 375 knots, the value of δ_c/δ_c may be read from Figure 4. As there defined, $\gamma_1 = (375/350)^{\frac{1}{2}} \times 1.148$, so that at 375 knots, 12,000 feet = $\frac{12,000}{2}$ \times x = 10,450 x feet. The point 9 determined by this slant range and 80° day. dive angle lies between the curves marked 10m and 15m, elightly nearer the latter, so that approximately $\delta_c/\delta_c = 13m = 16.9$ ft. per 5. The -15.05 adjustment in γ_c therefore displaces the impact point by about $\delta_c = 220$ feet.

The resultant impact error at (S_i, O_i, V_i) is then

i.e., the bomb may be expected to fail 150 feet beyond the target under the given conditions.

The effect of angle of ettack variation may be seen to be of considerable importance. If \mathcal{S}_{a} were neglected in this example, (b) and (c) alone would yield an impact error of f00 feet, or only 40% of that given by (14). Quite often even the algebraic eigh of the resultant error is changed by this effect.

[·] Determined by extending line VII and using lower extension scale.

According to the wording of the hypothesis, this example may at first appear to typify only the integrator adjustment method. But if the original misalignment were given not so -20 but as -30 mile, of which 10 mile were corrected by a sight adjustment and the balance by an integrator adjustment, the eclution would be identical, yet the problem would appear more general, involving a combination of eight and integrator adjustments. 4 The above example illustrates the method of determination of the ext mt to which a fixed adjustment fails to offset a sight micalignment at reagon, dive angles, and air speeds other than the central value The mode and extent of variation of this refor which the adjustment is made. eidual impact error with range, dive angle, and air speed is illustrated in Figuree 5. 7 and 8. for both the eight and integrator adjustment methode and various combinations of the two. In these graphs are plotted the results of fixed adjustments so determined as to eliminate completely the effect of the eight error at the model values S = 7500 feet, $\alpha = 40^{\circ}$, V = 350 knots, as in the example above. They are based on Figures 2 - 5 and on the formulae underlying them. Explanation of the derivation, inderpretation, and use of Figures 5, 7, and 8 follows:

At $\alpha = \alpha$ and v = V, let ϕ be that portion of the original eight error which remains after any direct eight adjustment is made; ϕ is then the error to be offset by an integrator adjustment. If this latter adjustment consists of a change in $T_{\mathcal{L}}$ in the ratio $\mathcal{L}_{\mathcal{L}}$, then by (9).

$$\mathcal{E}_{\rho} = \phi \cdot \bar{\Theta}_{\rho} \tag{15}$$

where \odot is the value of \odot when $S:S, \bowtie^2 \sigma$, and $\forall x \vec{v}$. As determined in the example, $\odot = 0.785$ per mil.

At any other value of S, ϕ , and V, the error S on the ground consists of three components analogous to those lettered (a), (b), (c), in the example above: (a) By (2) and (13), the impact displacement due to change $\Delta \phi_Q$ in angle of attack is

$$S_a = -5 \Delta d_a \cos \alpha = -\frac{5 CW}{\Delta m \alpha} \left(\frac{\cos \alpha}{V^2} - \frac{\cos \alpha}{V^2} \right)$$
 (160)

where C, W, ϕ and V are known constants. (b) Again by (2), that due to the model eight error ϕ alone is

$$\mathcal{L}_{\phi} = -5 \cdot \phi \operatorname{cse} \alpha \tag{16b}$$

(c) Finelly, by (4) and (15), that due to the integrator adjustment & alone is.

The resultant error of is the sum of (16a), (16b), and (16c):

where $\Delta \phi_{a}$ is a function of \nearrow and \bigvee , and $\stackrel{\bullet}{\textcircled{a}}$ is a constant,

When the entire correction is made through a sight adjustment, then $\varphi \equiv O$ and hence $\hat{g} \equiv \hat{g}_{\alpha}$ as given by (16a). Figure 6 is a contour map of \hat{g}_{α} as function of release point, for air speeds 350 \pm 35 knots, for an FeF plane (at nominal weight) whose sight is adjusted for $\hat{q} = 40^\circ$ and $\hat{\varphi} = 350$ knots. It will be noted that the curves for any one air speed approach parallelism in the direction corresponding to the dive angle Cafor which $\hat{q}_{\alpha} = 0$ at that air speed — i.s., for which $\hat{c}_{\alpha} = \sqrt{\frac{2}{3}} \frac{2000^{\circ}}{3000^{\circ}} (3500 \text{ knots})^{\circ}$. While constructed on the basis of FeF data, the errors given by Figure 6 are accurate to within 5% for the SB2C, and to within 15% for the TPM and F4U. The actual value of \hat{g}_{α} for any type of plane is obtainable from Figure 6 and the relation

which follows from (16a).

When, on the other hand, part or all of the correction is made through an integrator adjustment (\mathcal{E}_{c}), \mathcal{E}_{c} to the sum of this \mathcal{E}_{c} , esplotted in Figure 6, and an error $\Delta \mathcal{E}_{c}$ and \mathcal{E}_{c} are in a point and \mathcal{E}_{c} and \mathcal{E}_{c} are in a point \mathcal{E}_{c} and \mathcal{E}_{c} and is therefore the locus of \mathcal{E}_{c} and \mathcal{E}_{c} and is therefore the locus of \mathcal{E}_{c} and \mathcal{E}_{c} and is therefore the locus of \mathcal{E}_{c} and \mathcal{E}_{c} and is therefore the locus of \mathcal{E}_{c} and \mathcal{E}_{c} and is therefore the locus of \mathcal{E}_{c} and \mathcal{E}_{c} and

The recidual error of far the general sace is given by the sum of the errore as given in Figures 6 and 7, the latter being a function of the sight misalignment of the which the integrator adjustment is applied. When the sight likely is adjustable, of any be given any pre-determined value by means of a preliminary sight adjustment. Figure 8 is a set of contours of of obtained by combining Figures 6 and 7, for different values of of between -20 and 420 mile. The scale is the same as in Figures 6 and 7, but ranges and dive angles suiteids the most probable operating limits are excluded in order to facilitate analysis of the errors likely to be encountered in practice. The central graph (a), which is for of 0 to 1, is identical with Figure 6, except that the contour interval used in Figure 8 is 50 feet.

The complete colution of the above example is obtainable from Figures 6, 7, and 8. The point Q in Figures 6, 7, and 8(a) represents ($S_1 = 12,000$ feet, $C_1 = 60^{\circ}$). Interpolation between consecutive error curves for $C_1 = 375$ kmots, with $C_2 = -20$ mile, gives respectively $C_2 = 490$ feet, $C_3 = 60^{\circ}$ for $C_4 = 60^{\circ}$ mile) = 60° feet, $C_5 = 60^{\circ}$ feet, in exact agreement with the solution (14).

A study of Figure 8 sheds such light on the relative merits of the sight adjustment and integrator adjustment methods and of various exabinations thereof. The general trend of Figure 8 may be predicted from Figures 6 and 7,

The operating limits assumed here are so follows: Minimum dive angle 20° , minimum slant range, 4000 feet; maximum dive angle 60° , maximum second altitude 10,000 feet; and maximum slant range that which, according to Report 00.52:105 (Fig.2) would correspond to 100-foot borizontal error at 850 knots for Mod 0 bonb director. The point \tilde{P} (\tilde{S} = 7500 ft., \tilde{g} = 40°) is close to the "center of gravity" of this operating region.

When either Cl or V increases, according to Figures 6 and 7, S_{α} increases, whereas Δ 6 decreases or increases according as ϕ is positive or negative; these two error components therefore partially offset each other, as regards variation with α and V, when ϕ is positive, but increase the total error when ϕ is negative. This observation is borns out quantitatively by Figure 8. At ϕ = -20 ails (Figure 8s) the curves are densely packed, indicating wide variation of residual error; within the operating limits and for \pm 25-knot variation in V, S is seen to they approximately between -200 and ϕ 150 feet. As

 ϕ increases the curves become sparser, until at $\phi=420$ (Figure 8e) ϕ becomes practically independent of eir speed. At $\phi=410$ mils (Figure 8d), while being somewhat more dependent on eir speed, ϕ is limited to 480 feet throughout almost the entire operating region and at a fixed clant range seems to be almost independent of ϕ . The corresponding variation at $\phi=\phi$ (Figure 8e) is also between the limits of 450 feet, and more independent of slant range. In all three curves (c), (d) and (e), the worst error conditions occur in the vicinity of 30° and maximum range, the boxb falling chort by an assumt which approximates 100 feet. These results would, of course, be altered conservat if different values of ϕ , ϕ , and ϕ were used in the adjustment, but the general trend would be entirely similar.

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Aircraft whose sights are edjusted to be correct for machine gum use have eight similarments which average about -30 mile for toos booking. In view of Figure 8, correction of errors of euch magnitude by memme of an MPI $(\Delta T_C/T_C)$ adjustment alone is highly inadvisable, as this method makes the impact point very sensitive to changes in range, dive angle, and air speed. Adjustment of the eight itself brings much more bombing accuracy within wide limits, and seems to give an adjustment roughly independent of elent range.

Equally favorable results, however, may be achieved if a combination of sight and integrator adjustments is used. In this method the sight is over-adjusted until aired by about \$10 to \$20 mile, and this misalignment is in turn corrected by an NPI adjustment. The optimum sight adjustment depends on the choice of a model value of \$5.00, and \$V\$, but when these are 7500 fout, 400, and 350 knots, the minimum variation of impact error with dive angle is reached at an overadjustment of approximately \$10 mile; with air specifies at approximately \$20 mile; and with alant renge at approximately 0 mile (sight adjustment alone).

The effect of this combined edjustment is to offset the effect of changes in angle of attack by means of an integrator adjustment so determined as to counteract such variation. An additional advantage of this method line in the fact that, in practice, etermer dives are generally accompanied by g_{X_1} —terming speeds. Since an increase in either dive angle or air speed increases the error due to changes in angle of attack, it follows that a eight adjustment alone would note the impact point doubly sensitive to changes in ch or V. The combination method reduces the variation of c_1 with both c_2 and V. However,

1 . 17

^{*} Except for small dive angles.

if the minimation of the varietion of δ with slamt range at fixed values of α and V is considered more important, only the night adjustment, i.e., $\phi = 0$. should be made.

The above choice of modal values 5, \$\delta\$, whose which the adjustments are to be made, appears to be antisfactorily controlled with respect to usual operational limits. Any decrease in \$\delta\$ below 7500 feet would make positive values of \$\delta\$ \$/ \$\delta\$ (Figure 7) considerably more probable than negative values; and a light increase, perhaps to \$500 feet, would yield a somewhat better balanced distribution of errors.

In practice, however, greater accuracy in the sight adjustment is achieved at short ranges. Since angle of attack is independent of range, adjustment of the night at α , \overline{V} , and a range less than \overline{S} would not affect the result. The PI adjustment ($\Delta T_C / T_C$) could then be made at \overline{S} , $\overline{\alpha}$, and \overline{V} .

It is also recommended that this combination method of eight correction be tested in the field, to determine the agreement of theory and practice at different values of d. In any such tests, however, one doubles is by-lieved to be in order. The impact errors with which we are here concerned are comparable in magnitude with errors due to such factors as pilot mining and the use of approximate \(\psi \) -functions. A difference between two observed impact errors, for the same plane under different conditions, will be approximately free of components due to other factors, and is therefore much more reliable for this purpose than any single absolute observed error.

The results of this analysis, furthermore, de-emphasize the necessity for exact alignment of the flight and eight lines. An approximate alignment will generally suffice provided the error is on the side of over-adjustment, which is subsequently corrected through an NPI adjustment.

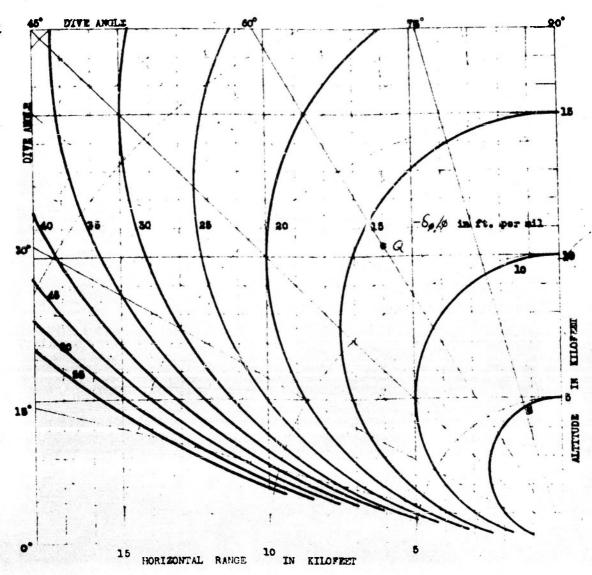
S. H. Lachenbruch

PLIGHT AND TRAJUCTORY DIAGRAN WITH MISALIGNED SIGHT Figure 1

Spatial Contour Map of: HORIZONTAL IMPACT ERROR (δ_ϕ) RESULTING FROM A GIVEN SIGHT ERROR (ϕ)

(Range-dive angle contours of constant ratio $\delta_{\phi/\phi}$, as indicated)

Independent of air speed (V) and of pull-up acceleration (K)



Pigure 2

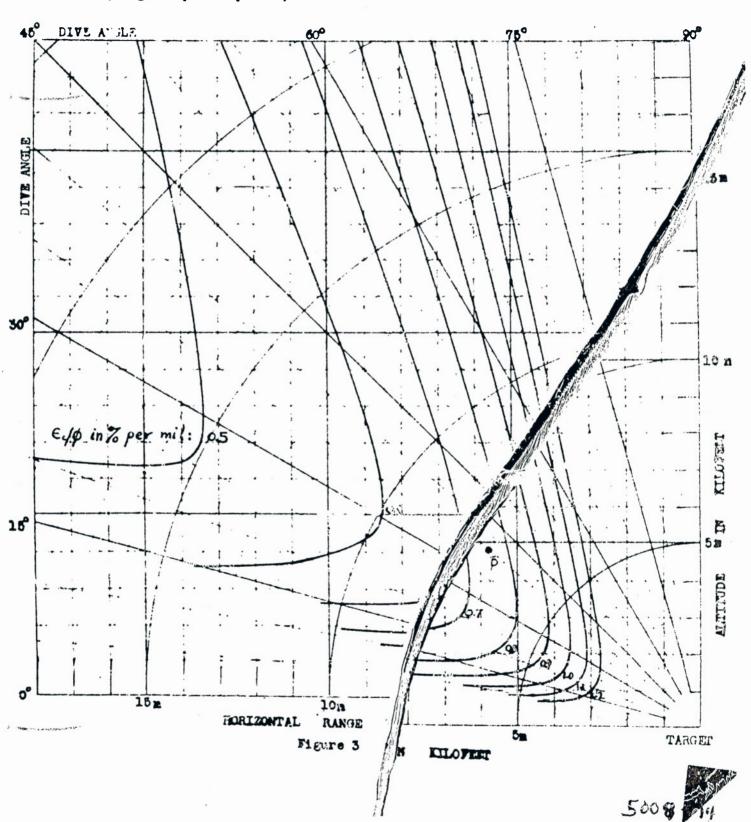
Spatial contour Map of:

MPI ADJUSTMENT (C). I.E., PERCENT CHANGE IN TIME TO TARDOT, REQUIRED TO OFFSET GIVEN SIGHT ERROR (ϕ)

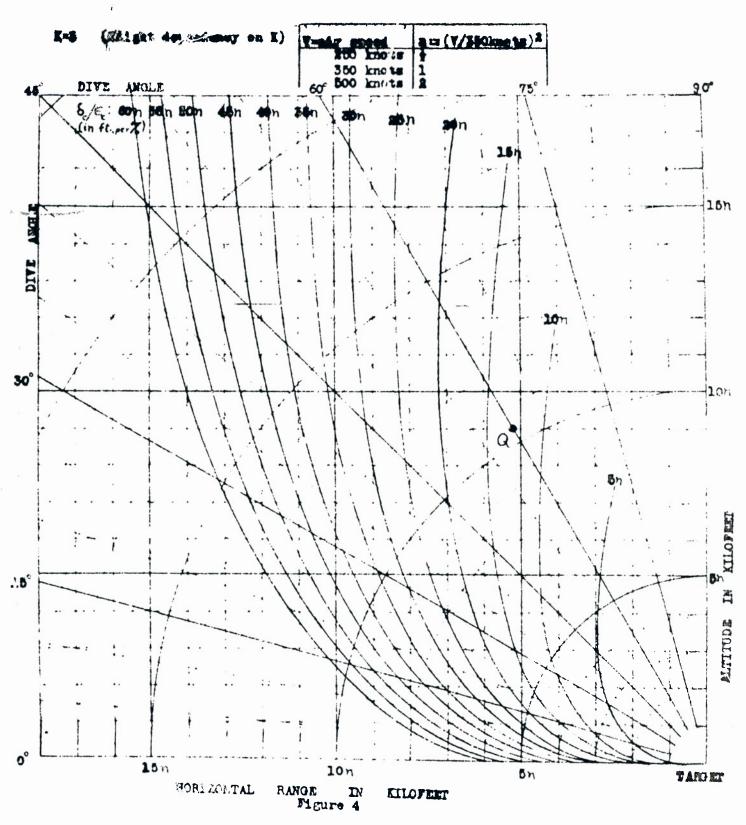
V.air	speed	n=(V/350knete)
100	200 16	Š.
350	knots	1
500	knets	2

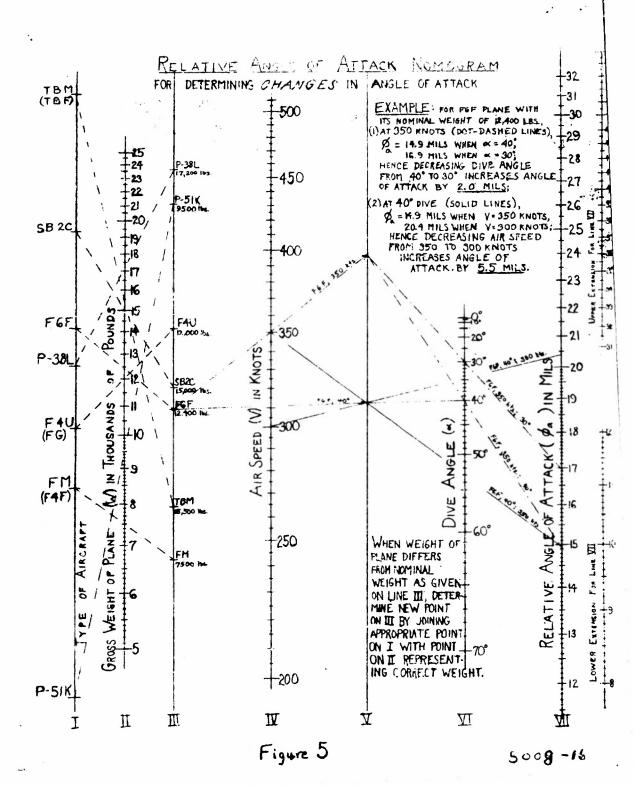
(Range-dive angle contours of constant ratio ϵ_{i}/ϕ)

(811ght dependency on X) **X-3**



(Range-Sive make continue of ensurement rante Science)





Spatial Centeur Map of: Horizonial impact in angle of attach, where sight is properly alligned at divergous 40° and air speed 350 knots.

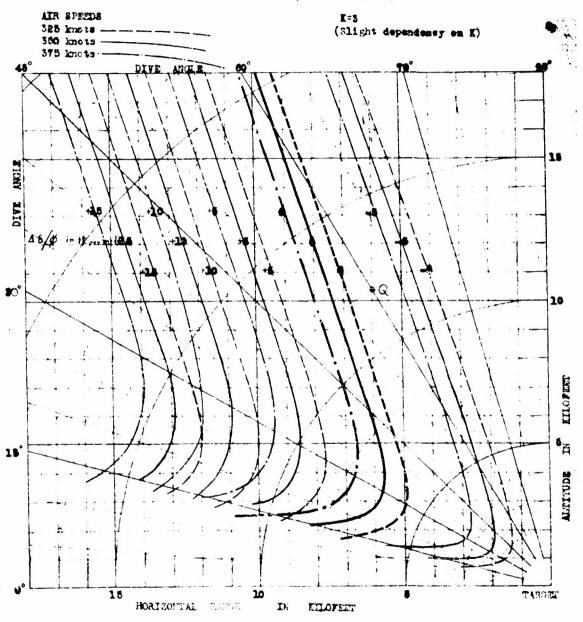
(Range-dive angle contours of constant δ_a , as indicated) Por Plane AIR SPEEDS Gross Wh.: 19400 1bs. 325 knets 350 knots (Independent of K) 375 knots DIVE ANGLE 15 Q. TARGET HORIZONTAL RANGE

Mgare 6

Spatial Contour Map of . NORIZONTAL IMPACT ERROR ($46=8_\phi+\delta_c$), NOT INCLUDING THAT DUE TO ANGLE OF ATTROCK, RESULTING FROM FIXED MPI ADJUSTMENT (ε_c) SO DETERMINED AS TO OFFSET A SIGHT

TROOK (ϕ) AT SLAWT RANGE 7.5 ELLOWEET. DIVE ANOLE 40°, AND AIRCPEED 550 ENOTS

(Range-dive angle contours of constant $\Delta\delta/\phi$, as indicated)



Tange-aive angle contours of ceratants, within orecritional li its,

given in units of

Spatial Contouring (Composite of Figures 6 77 of:

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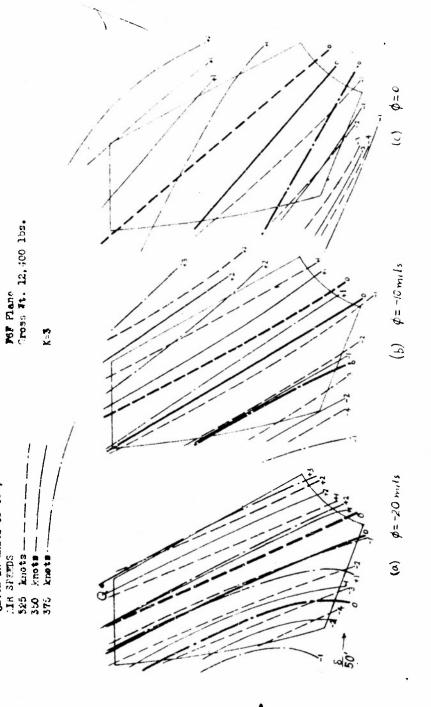
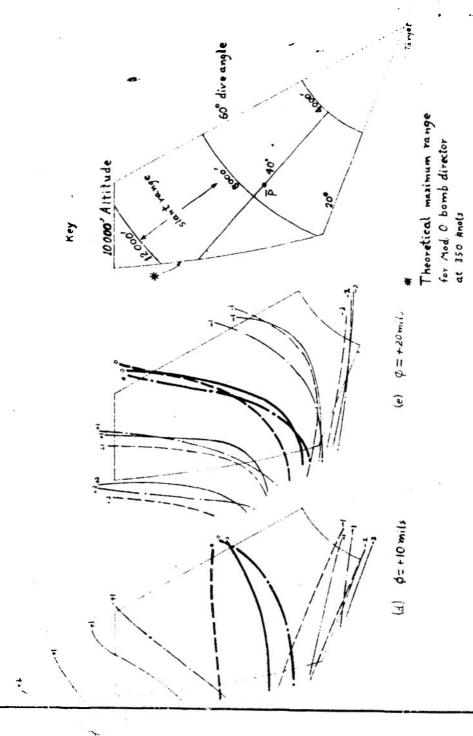


Figure 8



THE END

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